

Determinazione della numerosità campionaria

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Hydroxychloroquine and azithromycin as a treatment of COVID-19: results of an open-label non-randomized clinical trial ☆

2.10. Statistics

Assuming a 50% efficacy of hydroxychloroquine in reducing the viral load at day 7, an 85% power, a type I error rate of 5% and 10% loss to follow-up, we calculated that a total of 48 COVID-19 patients (ie, 24 cases in the hydroxychloroquine group and 24 in the control group) would be required for the analysis (Fleiss with CC). Statistical differences were evaluated by Pearson's chi-square or Fisher's exact tests as categorical variables, as appropriate. Means of quantitative data were compared using Student's t-test. Analyses were performed in Stata version 14.2.

La dimensione del campione

Stima (su considerazioni statistiche)

Giustificazione (su considerazioni economiche e biologiche)

Aggiustamento (in accordo a potenziali dropouts o effetti di covariate)

Perché stimare **a priori** la dimensione del campione da studiare?



Per assicurare che il numero di soggetti/pazienti coinvolti nello studio clinico permetta di rispondere adeguatamente al quesito di interesse, considerando che:

1. Uno studio di dimensioni limitate avrà un elevata probabilità di non riuscire a riconoscere un trattamento promettente;
2. Uno studio di dimensioni eccessive è economicamente oneroso e rischia di sottoporre un eccessivo numero di soggetti/pazienti ad un trattamento non efficace.

Patients I need = sample size

Patients I can get = power

Come si calcola la sample size?

Il calcolo della sample size varia a seconda di:

- **Obiettivo dello studio** (superiorità, inferiorità, etc);
- **Disegno dello studio** (gruppi paralleli, gruppi indipendenti, cross-over, etc), numero dei gruppi di trattamento da confrontare;
- **End-point primario** (percentuale di successo, probabilità di sopravvivenza libera da evento, livello medio di un parametro quantitativo, etc);
- **Parametri clinici** (entità dell'effetto, percentuale di drop-out, variabilità del fenomeno);
- **Parametri statistici** (tipo di test d'ipotesi, livello di significatività, potenza dello studio).

Power Analysis

Test for	Null Hypothesis	Alternative Hypothesis
Equality	$H_0 : \mu_T - \mu_S = 0$	$H_a : \mu_T - \mu_S \neq 0$
Non-inferiority	$H_0 : \mu_T - \mu_S \geq \delta$	$H_0 : \mu_T - \mu_S < \delta$
Superiority	$H_0 : \mu_T - \mu_S \leq \delta$	$H_0 : \mu_T - \mu_S > \delta$
Equivalence	$H_0 : \mu_T - \mu_S \geq \delta$	$H_0 : \mu_T - \mu_S < \delta$

Quali sono i fattori che entrano nel calcolo della sample size?

- Il **potere del test ($1-\beta$)** che si desidera ottenere (valori di riferimento standard sono l'80% e il 90%). Probabilità di rigettare l'ipotesi nulla quando esiste una reale differenza o associazione.
- La **differenza minima tra i trattamenti** che sia " clinicamente rilevante". Può essere espresso in generale come il grado di beneficio che il nuovo trattamento dovrebbe fornire rispetto a quello vecchio perché valga la pena di utilizzarlo. Negli studi di *superiorità* è la minima differenza clinicamente rilevante; negli studi di *non-inferiorità* massimo svantaggio clinicamente tollerabile
- Il **livello di significatività (α)**, cioè la probabilità di ottenere una differenza "statisticamente significativa" quando di fatto differenza non c'è.

Errori di I e II tipo

Medie della Popolazione
Uguali (H_0) Differenti (H_1)

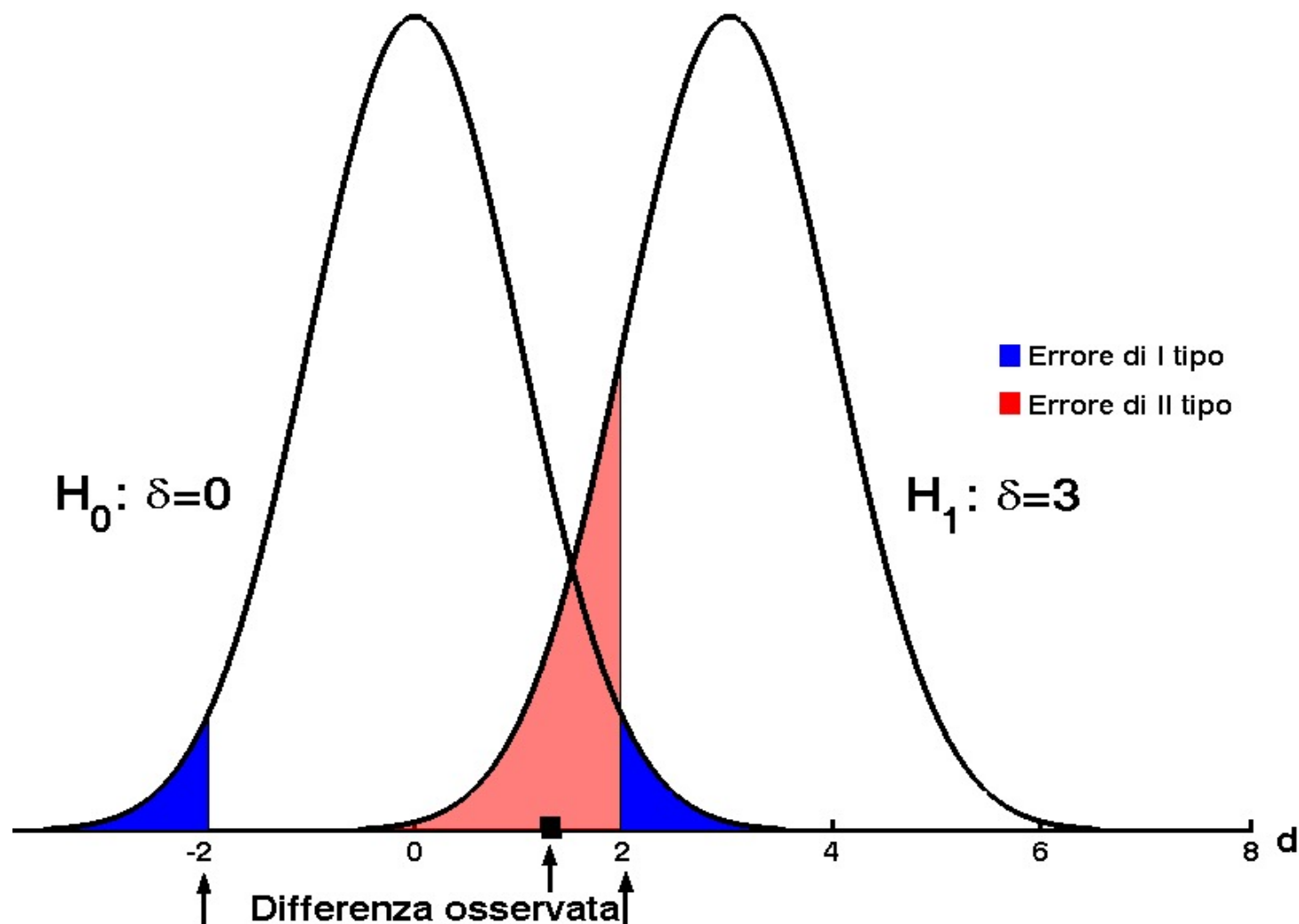
Conclusione Test

Le medie non
sono differenti

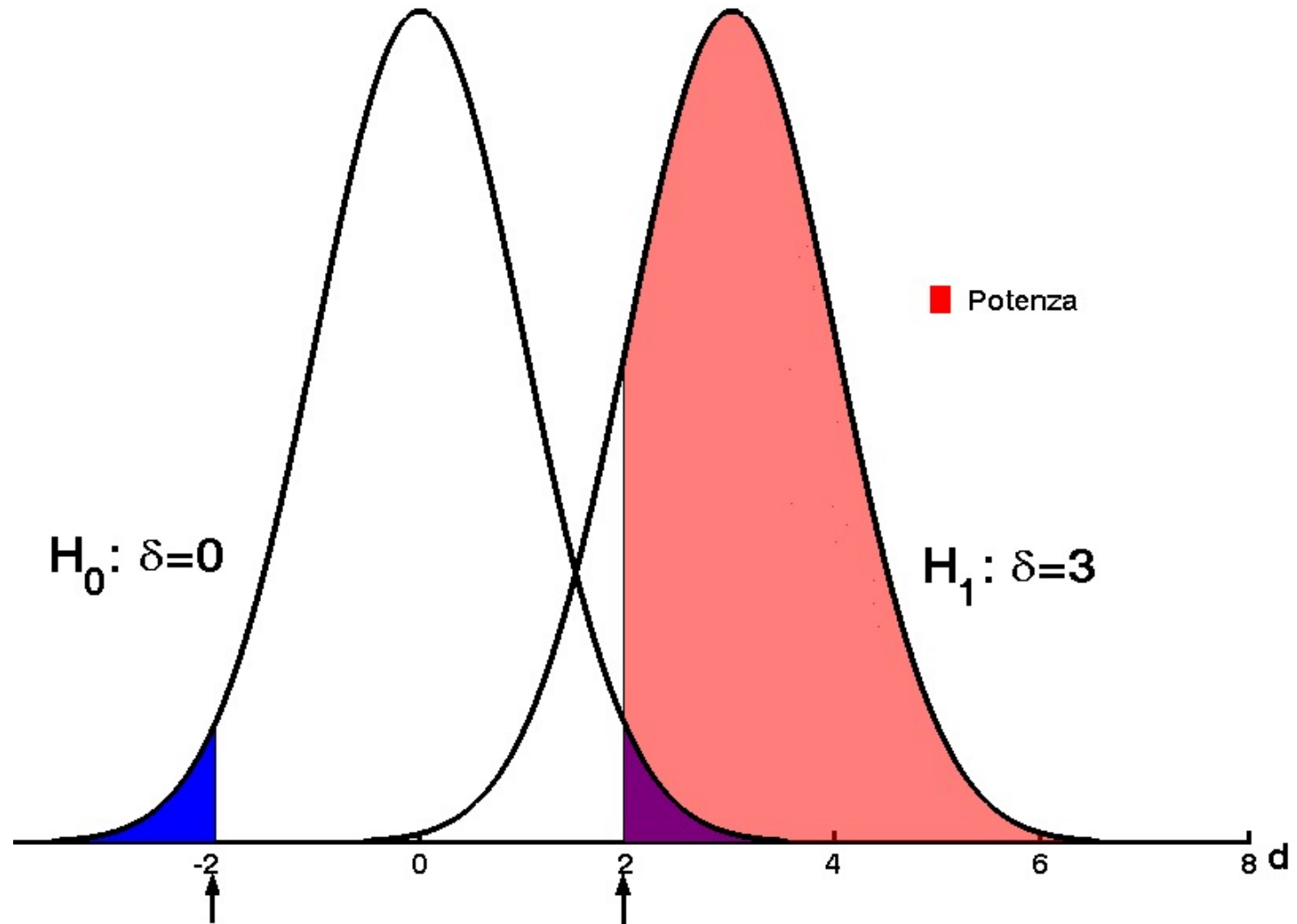
Le medie sono
differenti

VN	FN
II (β)	
FP	potenza ($1-\beta$)
I (α)	VP

Errori di I e II tipo



Potenza del test ($1 - \beta$)



Effetto della precisione sulla sample size

Per i valori più comuni di α e $1-\beta$

	<i>1-β</i>		
<i>α</i>	0,80	0,90	0,95
0,10	6,2	8,6	10,8
0,05	7,9	10,5	13,0
0,01	11,7	13,0	17,8

$$(Z_{\beta} + Z_{\alpha/2})^2$$

Variabili quantitative

$$n = \frac{2\sigma^2}{(\mu_1 - \mu_2)^2} (Z_\beta + Z_{\alpha/2})^2$$

! A posteriori è bene comparare la varianza dei dati osservati con quella utilizzata nella stima della sample size!

Variabili quantitative

Esempio: Il farmaco di riferimento riduce la pressione sistolica di 25 mmHg, il nuovo farmaco per essere competitivo dovrebbe ridurre la pressione sistolica di almeno 30 mmHg (ovvero 5 mmHg in più). La deviazione standard della riduzione della pressione viene stimata in 10 mmHg da studi precedenti. Si adotta un alfa del 5% e una potenza del 90%, pertanto $f(\alpha, \beta) = 10,5$

```
. sampsi 25 30, sd1(10) sd2(10) power(.9)
```

Estimated sample size for two-sample comparison of means

Test Ho: $m1 = m2$, where $m1$ is the mean in population 1
and $m2$ is the mean in population 2

Assumptions:

```
alpha = 0.0500 (two-sided)
power = 0.9000
m1 = 25
m2 = 30
sd1 = 10
sd2 = 10
n2/n1 = 1.00
```

Estimated required sample sizes:

```
n1 = 85
n2 = 85
```

Occorrono almeno 85 soggetti per gruppo.

Variabili qualitative

$$n = \frac{p_1(100 - p_1) + p_2(100 - p_2)}{(p_1 - p_2)^2} (Z_\beta + Z_{\alpha/2})^2$$

Variabili qualitative

Esempio: Nei pazienti affetti da tumore X in stadio avanzato, la sopravvivenza a 5 anni è del 30% con il trattamento standard. Dati preliminari suggeriscono che nei pazienti sottoposti ad un nuovo trattamento la sopravvivenza salga al 40%. Si adotta un alfa del 5% e una potenza dell' 80%, pertanto $f(\alpha, \beta) = 7,9$

```
. sampsi 0.30 0.40, power(.8)
```

Estimated sample size for two-sample comparison of proportions

Test Ho: $p_1 = p_2$, where p_1 is the proportion in population 1
and p_2 is the proportion in population 2

Assumptions:

```
alpha = 0.0500 (two-sided)
power = 0.8000
p1 = 0.3000
p2 = 0.4000
n2/n1 = 1.00
```

Estimated required sample sizes:

```
n1 = 376
n2 = 376
```

Occorrono almeno 376 soggetti per gruppo.

Variabili quantitative-Paired data

$$n = \frac{\sigma_D^2 (Z_\beta + Z_{\alpha/2})^2}{\bar{D}^2}$$

```
. sampsi 498 485, sd1(20.2) sd2(19.5) method(change) pre(1) post(3) r1(.7)
```

Estimated sample size for two samples with repeated measures

Assumptions:

alpha =	0.0500	(two-sided)
power =	0.9000	
m1 =	498	
m2 =	485	
sd1 =	20.2	
sd2 =	19.5	
n2/n1 =	1.00	
number of follow-up measurements =	3	
correlation between follow-up measurements =	0.700	
number of baseline measurements =	1	
correlation between baseline & follow-up =	0.700	

Method: **CHANGE**

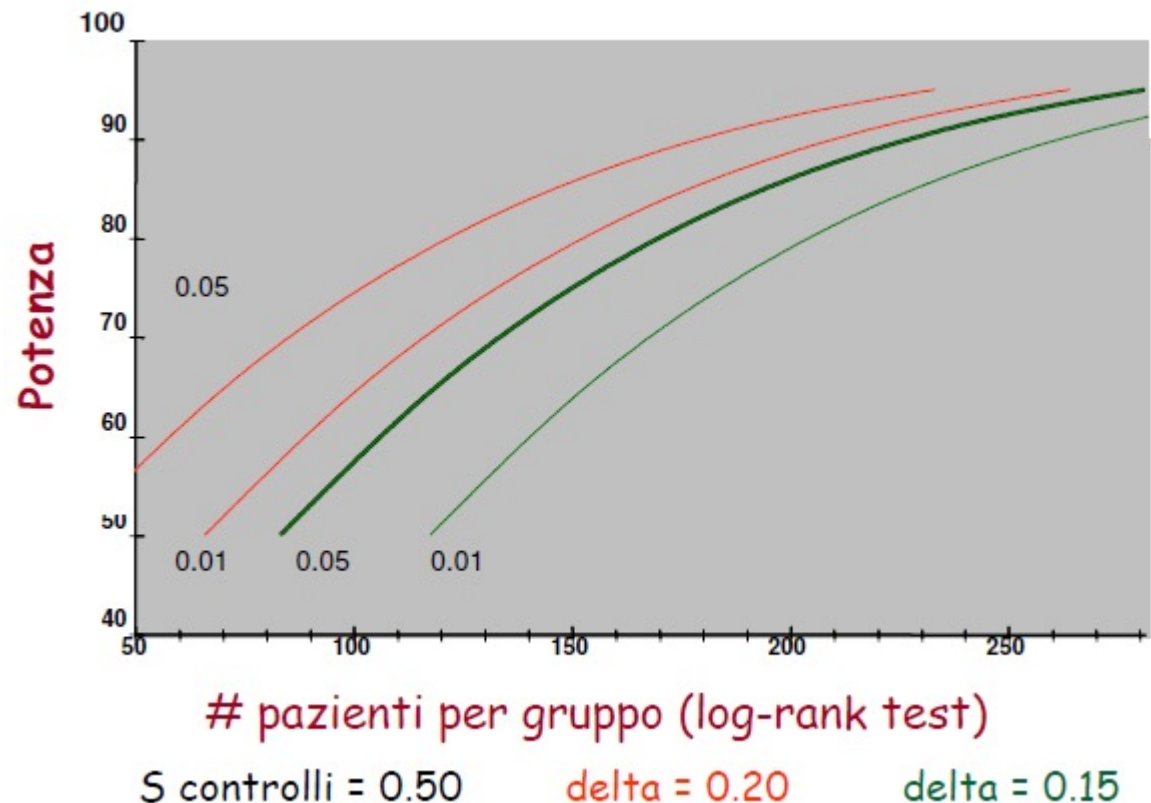
relative efficiency =	2.500
adjustment to sd =	0.632
adjusted sd1 =	12.776
adjusted sd2 =	12.333

Estimated required sample sizes:

n1 =	20
n2 =	20

Factors Affecting sample size

- I livelli di errore
- La misura dell'effetto (delta)
- La deviazione standard del fenomeno



Design	Hypothesis	Hypotheses and Sample Size Rules		
		H_0	H_a	Basic Rule
One-sample	Equality	$\mu - \mu_0 = 0$	$\mu - \mu_0 \neq 0$	$n = \frac{(z_{\frac{\alpha}{2}} + z_{\beta})^2 \sigma^2}{(\mu - \mu_0)^2}$
	Superiority	$\mu - \mu_0 \leq \delta$	$\mu - \mu_0 > \delta$	$n = \frac{(z_{\alpha} + z_{\beta})^2 \sigma^2}{(\mu - \mu_0 - \delta)^2}$
	Equivalence	$ \mu - \mu_0 \geq \delta$	$ \mu - \mu_0 < \delta$	$n = \frac{(z_{\alpha} + z_{\beta})^2 \sigma^2}{(\mu - \mu_0 - \delta)^2}$
Two-sample Parallel	Equality	$\mu_1 - \mu_2 = 0$	$\mu_1 - \mu_2 \neq 0$	$n_i = \frac{2(z_{\frac{\alpha}{2}} + z_{\beta})^2 \sigma^2}{(\mu_1 - \mu_2)^2}$
	Non-inferiority	$\mu_1 - \mu_2 \geq \delta$	$\mu_1 - \mu_2 < \delta$	$n_i = \frac{2(z_{\alpha} + z_{\beta})^2 \sigma^2}{(\mu_1 - \mu_2 - \delta)^2}$
	Superiority	$\mu_1 - \mu_2 \leq \delta$	$\mu_1 - \mu_2 > \delta$	$n_i = \frac{2(z_{\alpha} + z_{\beta})^2 \sigma^2}{(\mu_1 - \mu_2 - \delta)^2}$
	Equivalence	$ \mu_1 - \mu_2 \geq \delta$	$ \mu_1 - \mu_2 < \delta$	$n_i = \frac{2(z_{\alpha} + z_{\beta})^2 \sigma^2}{(\mu_1 - \mu_2 - \delta)^2}$
Two-sample Crossover	Equality	$\mu_1 - \mu_2 = 0$	$\mu_1 - \mu_2 \neq 0$	$n_i = \frac{(z_{\frac{\alpha}{2}} + z_{\beta})^2 \sigma^2}{2(\mu_1 - \mu_2)^2}$
	Non-inferiority	$\mu_1 - \mu_2 \geq \delta$	$\mu_1 - \mu_2 < \delta$	$n_i = \frac{(z_{\alpha} + z_{\beta})^2 \sigma^2}{2(\mu_1 - \mu_2 - \delta)^2}$
	Superiority	$\mu_1 - \mu_2 \leq \delta$	$\mu_1 - \mu_2 > \delta$	$n_i = \frac{(z_{\alpha} + z_{\beta})^2 \sigma^2}{2(\mu_1 - \mu_2 - \delta)^2}$
	Equivalence	$ \mu_1 - \mu_2 \geq \delta$	$ \mu_1 - \mu_2 < \delta$	$n_i = \frac{(z_{\alpha} + z_{\beta})^2 \sigma^2}{2(\mu_1 - \mu_2 - \delta)^2}$

Design	Hypothesis	Hypotheses and Sample Size rules	
		H_0	Basic Rule
One-sample	Equality	$\pi - \pi_0 = 0$	$n = \frac{(z_{\frac{\alpha}{2}} + z_{\beta})^2 \pi(1-\pi)}{(\pi - \pi_0)^2}$
	Superiority	$\pi - \pi_0 \leq \delta$	$n = \frac{(z_{\alpha} + z_{\beta})^2 \pi(1-\pi)}{(\pi - \pi_0 - \delta)^2}$
	Equivalence	$ \pi - \pi_0 \geq \delta$	$n = \frac{(z_{\alpha} + z_{\beta})^2 \pi(1-\pi)}{(\pi - \pi_0 - \delta)^2}$
Two-sample Parallel	Equality	$\pi_1 - \pi_2 = 0$	$n_i = \frac{(z_{\frac{\alpha}{2}} + z_{\beta})^2 (\pi_1(1-\pi_2) + \pi_2(1-\pi_1))}{(\pi_1 - \pi_2)^2}$
	Non-inferiority	$\pi_1 - \pi_2 \geq \delta$	$n_i = \frac{(z_{\alpha} + z_{\beta})^2 (\pi_1(1-\pi_2) + \pi_2(1-\pi_1))}{(\pi_1 - \pi_2 - \delta)^2}$
	Superiority	$\pi_1 - \pi_2 \leq \delta$	$n_i = \frac{(z_{\alpha} + z_{\beta})^2 (\pi_1(1-\pi_2) + \pi_2(1-\pi_1))}{(\pi_1 - \pi_2 - \delta)^2}$
	Equivalence	$ \pi_1 - \pi_2 \geq \delta$	$n_i = \frac{(z_{\alpha} + z_{\beta})^2 (\pi_1(1-\pi_2) + \pi_2(1-\pi_1))}{(\pi_1 - \pi_2 - \delta)^2}$
Two-sample Crossover	Equality	$\pi_1 - \pi_2 = 0$	$n_i = \frac{(z_{\frac{\alpha}{2}} + z_{\beta})^2 \sigma_d^2}{2(\pi_1 - \pi_2)^2}$
	Non-inferiority	$\pi_1 - \pi_2 \geq \delta$	$n_i = \frac{(z_{\alpha} + z_{\beta})^2 \sigma_d^2}{2(\pi_1 - \pi_2 - \delta)^2}$
	Superiority	$\pi_1 - \pi_2 \leq \delta$	$n_i = \frac{(z_{\alpha} + z_{\beta})^2 \sigma_c^2}{2(\pi_1 - \pi_2 - \delta)^2}$
	Equivalence	$ \pi_1 - \pi_2 \geq \delta$	$n_i = \frac{(z_{\alpha} + z_{\beta/2})^2 \sigma_d^2}{2(\pi_1 - \pi_2 - \delta)^2}$

Sample size adjustments



- Separate sample size calculation should be done for each important outcome & then use the max. estimate
- When two variables are correlated with a factor p , then sample size can be reduced by a factor of $1-p^2$
- Another option is to use Bonferroni correction for multiple outcomes

Sample size adjustments



- Allowing for response rates & other losses to the sample
 - The expected response rate
 - Loss to f/u
 - Lack of compliance
 - Other losses

$$n_{new} = n / (1 - L)$$

when L is the loss to f/u rate

Sample size adjustments



Adjustment for unequal group size

- Assuming $n_1/n_2=k$
- Calculate n assuming equal
- Then

$$n_2=0.5n(1+1/k)$$

$$n_1=0.5n(1+k)$$

Reporting Sample Size Calculations

- Clear statement of the **primary objective**
- The desired **level of significance**
- The desired **power**
- The **statistics methods** that will be used for analysis
- Whether the test would be **one or two-tailed**
- The smallest difference
 - Smallest clinically important difference
 - The difference that investigators think is worth detecting
 - The difference that the investigators think is likely to be detected

Reporting Sample Size Calculations

- **Justification** for prior estimates used in calculations
- Clear statements about the assumptions made about the distribution or **variability** of the outcomes
- Clear statement about the **scheduled** duration of the study
- Statement about how the sample size was **adjusted**
- The **software or formulae** that was used

Strategies For Maximizing Power & Minimizing the Sample Size

- Use common outcomes (the power is driven more by the number of events than the total sample size)
- Use paired design (such as cross-over trial)
- Use continuous variables
- Choose the timing of the assessments of primary outcomes to be when the difference is most likely to be optimal

Online free software available

<http://www.stat.ucla.edu/~jbond/HTMLPOWER/index.html>

<http://www.health.ucalgary.ca/~rollin/stats/ssize/>

<http://www.stat.uiowa.edu/%7Erlenth/Power/index.html>

<http://www.dssresearch.com/SampleSize/>

<http://www.stat.ucla.edu/calculators/powercalc/>

http://hedwig.mgh.harvard.edu/sample_size/size.html

<http://www.bobwheeler.com/stat/SSize/ssize.html>

<http://www.math.yorku.ca/SCS/Online/power/>

<http://www.surveysystem.com/sscalc.htm>

<http://www.researchinfo.com/docs/calculators/samplesize.cfm>

Sample Sizes for Time-to-Event Studies

Outcome Measure	Examples of Associated Time-to-Event Measure
Death	Survival Time
Response (Tumor shrinkage)	Duration of response
Recurrence of disease	Time to recurrence
Relief of symptoms	Time to relief of symptoms/without symptoms
Quality of life 'scores'	Time to improvement/deterioration in scores
Toxicity	Time with/without toxicity

M_t = mean survival time in Treatment Group

M_c = mean survival time in Control Group

$$n = \frac{2 \left(Z_{\alpha/2} + Z_{\beta} \right)^2}{\left(\ln(M_t/M_c) \right)^2}$$

- Most software require the use of event-free rates (survival) and not event rates (death), because the log rank test is based on event-free rates
- Beware if your software is giving you total **number of subjects or events**.