

**ESERCIZIO 1:** Calcolare il limite per  $n \rightarrow +\infty$  delle seguenti successioni:

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| $\{a_n\}_{n \in \mathbb{N}} = \left\{ \left( \frac{n^2}{5n + n^2 + 3} \right) \right\}_{n \in \mathbb{N}}$   | $\{b_n\}_{n \in \mathbb{N}} = \left\{ 2n^2 \ln \left( 1 + \frac{1}{n^2} \right) \right\}_{n \in \mathbb{N}}$         |
| $\{a_n\}_{n \in \mathbb{N}} = \left\{ \left( \frac{n+2}{n^3+4} + 1 \right) \right\}_{n \in \mathbb{N}}$      | $\{a_n\}_{n \in \mathbb{N}} = \left\{ \ln \left( \frac{5n+3n^2}{1+2n} \right) \right\}_{n \in \mathbb{N}}$           |
| $\{a_n\}_{n \in \mathbb{N}} = \left\{ \left( \frac{4^{n+1} - 1}{3^n} \right) \right\}_{n \in \mathbb{N}}$    | $\{b_n\}_{n \in \mathbb{N}} = \left\{ \left( \frac{1}{3} \right)^{\frac{3n^2+4}{1+n}} \right\}_{n \in \mathbb{N}}$   |
| $\{a_n\}_{n \in \mathbb{N}} = \left\{ \left( \frac{3+2^n}{3^n} \right) \right\}_{n \in \mathbb{N}}$          | $\{b_n\}_{n \in \mathbb{N}} = \left\{ \left( 1 + \frac{7}{n^2} \right)^{5n^2} \right\}_{n \in \mathbb{N}} \quad (*)$ |
| $\{a_n\}_{n \in \mathbb{N}} = \left\{ \left( \frac{3+3^n}{5^n} \right) \right\}_{n \in \mathbb{N}}$          | $\{b_n\}_{n \in \mathbb{N}} = \left\{ \left( 1 + \frac{1}{2+n} \right)^{3n} \right\}_{n \in \mathbb{N}} \quad (*)$   |
| $\{a_n\}_{n \in \mathbb{N}} = \left\{ \ln(n^2 - 3) - \ln(1 + n^2) \right\}_{n \in \mathbb{N}}$               | $\{b_n\}_{n \in \mathbb{N}} = \left\{ \frac{3n^2 + 2n - 5}{3 - n} \right\}_{n \in \mathbb{N}}$                       |
| $\{a_n\}_{n \in \mathbb{N}} = \left\{ \ln \left( \frac{5-3n}{2-n} \right) \right\}_{n \in \mathbb{N}}$       | $\{b_n\}_{n \in \mathbb{N}} = \left\{ \frac{5+2n}{1+2n+n^2} \right\}_{n \in \mathbb{N}}$                             |
| $\{a_n\}_{n \in \mathbb{N}} = \left\{ \left( \frac{-3^n + 1}{6^{n+1}} \right) \right\}_{n \in \mathbb{N}}$   | $\{b_n\}_{n \in \mathbb{N}} = \left\{ \frac{n^2 + n + 1}{(n+1)^2} \right\}_{n \in \mathbb{N}}$                       |
| $\{a_n\}_{n \in \mathbb{N}} = \left\{ \left( \frac{2^{2n} + 1}{3^n} \right) \right\}_{n \in \mathbb{N}}$     | $\{b_n\}_{n \in \mathbb{N}} = \left\{ \frac{n}{n-1} + \frac{5n^2 - 4}{6n + 2} \right\}_{n \in \mathbb{N}}$           |
| $\{a_n\}_{n \in \mathbb{N}} = \left\{ \left( \frac{n+1}{n} \right)^n \right\}_{n \in \mathbb{N}}$            | $\{b_n\}_{n \in \mathbb{N}} = \left\{ \frac{n^2 - 6n + 1}{6n^3 - 4n + 2} \right\}_{n \in \mathbb{N}}$                |
| $\{a_n\}_{n \in \mathbb{N}} = \left\{ \left( \frac{n}{n-1} \right)^n \right\}_{n \in \mathbb{N}} \quad (**)$ |  |

**ESERCIZIO 2:** Calcolare i seguenti limiti:

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| $\lim_{n \rightarrow +\infty} \frac{n^3 - 1}{(n+1)(n^2 + 2n)}$ | $\lim_{n \rightarrow +\infty} \left(\frac{1}{5}\right)^{\frac{2n-1}{3-n}}$ |
| $\lim_{n \rightarrow +\infty} \frac{n}{n^3 + 2n}$              | $\lim_{n \rightarrow +\infty} \frac{3n^2 + 5}{n^2 - 2n + 1}$               |
| $\lim_{n \rightarrow +\infty} \frac{n^2 - 4n^3}{2 + n^3}$      | $\lim_{n \rightarrow +\infty} n \ln \left(1 + \frac{2}{n^3}\right)^{n^2}$  |
| $\lim_{n \rightarrow +\infty} \frac{5^{n-2} + 4}{4^{2n}}$      | $\lim_{n \rightarrow +\infty} e^{-n+1}$                                    |
| $\lim_{n \rightarrow +\infty} \frac{2^n - 4}{3^{n+1}}$         |  |